Multiple scattering effects in Glauber model descriptions of single-nucleon removal reactions

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The Glauber/eikonal model is a widely used tool for study of intermediate- and high-energy nuclear reactions. When calculating the Glauber/eikonal model phase-shift functions, the optical limit approximation (OLA) is often used. The OLA neglects the multiple scattering of the constituent nucleons in the projectile and the target nuclei. On the other hand, the nucleon-target version of the Glauber model (the NTG model) proposed by B. Abu-Ibrahim and Y. Suzuki includes multiple scattering effects between the projectile nucleons and the target nuclei. The NTG model has been found to improve the description of the elastic scattering angular distributions and the total reaction cross sections of some light heavy-ion systems with respect to the OLA. In this work, we study the single-nucleon removal reactions (SNRR) induced by carbon isotopes on 12 C and 9 Be targets using both the NTG model and the OLA. Reduction factors (RFs) of the single nucleon spectroscopic factors are obtained by comparing the experimental and theoretical SNRR cross sections. It is found that, on average, the RFs obtained with the NTG model is smaller than those using the OLA by 7.8%, in which, the averaged differences in one-neutron removal is 10.6% and those in one-proton removal is 4.2%. But the RFs still have a strong dependence on the neutron-proton asymmetry ΔS of the projectile nuclei even when the NTG model is used.

Keywords: Glauber model of nuclear reactions, single-nucleon removal reactions, spectroscopic factors

I. INTRODUCTION

Measurements and theoretical analysis of single-nucleon 3 removal reactions are of great value for studies of single-4 particle strengths of atomic nuclei, which are quantitatively 5 represented by spectroscopic factors (SFs) [1]. It is wellβ known that the SFs extracted from (e, e'p) and single-nucleon $_{7}$ transfer reactions are found to be 30% - 50% smaller 8 than those predicted by configuration interaction shell model 9 (CISM) [2, 3]. Such reduction or quenching of SFs, repre-10 sented by the quenching factors, R_s , is supposed to be orig-11 inated from the limited model spaces and insufficient treat-₁₂ ment of the nucleon-nucleon correlations in the traditional 13 CISM [4, 5]. Unlike the results from (e, e'p) reactions, 14 from single-nucleon transfer reactions, and from (p, 2p) and 15 (p, pn) reactions [2, 3, 6, 7], where the R_s values of different 16 nuclei are nearly constant, the quenching factors from inter-17 mediate energy single-nucleon removal reactions are found to 18 depend almost linearly with the proton-neutron asymmetry of 19 the atomic nuclei, ΔS ($\Delta S = S_p - S_n$ for proton removal 20 and $\Delta S = S_n - S_p$ for neutron removal with S_n and S_p being the neutron and proton separation energies in the ground states of the projectile nuclei, respectively) [8, 9]. For cases when ΔS is larger than around 20 MeV, which correspond to $_{
m 24}$ removal of strongly bound nucleons, the R_s values decrease $_{\text{25}}$ to about 0.3; however, when ΔS is smaller than around -20 26 MeV, which corresponds to removal of weakly-bound nucle- $_{27}$ ons, the R_s values are close to unity. The reasons why such 28 a clear linear dependence is seen in results of intermediate-²⁹ energy single-nucleon removal reactions are still not known.

³⁰ Since most of the single-nucleon removal reactions are ana-³¹ lyzed with the Glauber model, validity of the eikonal/Glauber ³² model [8–10] has been put under question [11].

Because of its simplicity, the optical limit approximation (OLA) is often used in the eikonal/Glauber model analy-35 sis of the intermediate- and high-energy nuclear reactions 36 [10, 12, 13]. Only the first-order term of the expansion of the 37 full Glauber phase shift is taken into account with the OLA. 38 Higher-order interactions, such as the nucleon-nucleon mul-39 tiple scattering processes are neglected [14]. In Ref. [15], B. 40 Abu-Ibrahim and Y. Suzuki found that although the Glauber 41 model with the OLA can reasonably reproduce the total re-42 action cross sections of some stable ions on ⁹Be, ¹²C, ²⁷Al 43 targets, it failed to reproduce the reaction cross sections and 44 elastic scattering angular distributions of unstable nuclei. For 45 this, they proposed to calculate the projectile-target phase shifts using nucleon-target interactions in Glauber model calculations. This so-called NTG model (nucleon-target version 48 of the Glauber model) has been found to improve the descrip-49 tion of the reaction cross sections and the elastic scattering 50 angular distributions data considerably [15–17]. However, to our knowledge, application of the NTG model to the analysis 52 of single-nucleon knockout reactions and to study its influ-53 ence on the reduction factors of single particle strengths has not been made yet. In this work, we study how much the R_s values of single-nucleon knockout reactions change when the NTG model is used instead of the usual OLA. Since the NTG 57 model includes multiple scattering effects in the phase-shift functions of the colliding systems with respect to the OLA, we expect this work may give us information about how much 60 the multiple scattering effects will affect the description of 61 single nucleon removal reactions using the Glauber model.

This paper is organized as the following: the NTG model and the OLA of the Glauber model are briefly introduced in

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 $_{65}$ which include 1) examination of the NTG model about its $_{108}$ range of the NN interaction is smaller than the radius of the 66 reproduction of the elastic scattering and total reaction cross 109 target nucleus, which is satisfied in most cases, the integral section data. The cases studied are the angular distributions of $110 \int d\mathbf{r} n_i(\mathbf{r}) \Gamma_{NN}(\mathbf{b} - \mathbf{t})$ will be smaller than unity [14]. Then ¹²C elastic scattering from a carbon target at incident energies 111 the following approximation could be made [14]: 69 from 30 to 200 MeV/u and the ¹²C+¹²C total reaction cross 70 sections from 20 to 1000 MeV/nucleon, 2) detailed study of 71 the NTG model on single-nucleon removal at different in-72 cident energies, the case studied here is the ${}^{9}\text{Be}({}^{19}\text{C}, {}^{18}\text{C})\text{X}$ 73 reaction, and 3) effects of the NTG model on the reduc-74 tion factors of the single particle strengths. The cases stud-75 ied are single nucleon removal cross sections of carbon iso-76 topes $9{,}10{,}12{-}20$ C on 9Be and carbon targets within 43-250 77 MeV/nucleon incident energies. The range of ΔS covered in 78 these reactions is from -26.6 to 20.1 MeV. All results are compared with those of the OLA calculations in order to explicate 115 80 the influence of multiple scattering effects in these reactions. The conclusions are given in section IV.

II. THE NTG MODEL AND THE OLA

The NTG model was introduced in Refs. [15, 16]. Details 84 of its formulae can be found in Ref. [14]. For the convenience 85 of the readers, we recapitulate the necessary ones here. Let us start from the phase-shift function of a nucleon-target system, 87 χ_{NT} , which is defined in the Glauber model framework as 88 [14]:

$$e^{i\chi_{NT}(\boldsymbol{b})} = \langle \Phi_0^{\mathrm{T}} | \prod_{j=1}^{A_{\mathrm{T}}} \left[1 - \Gamma_{NN}(\boldsymbol{b} - \boldsymbol{t}_j) \right] \Phi_0^{\mathrm{T}} \rangle, \quad (1)$$

where $m{b}$ is the impact factor vector, $m{t}_j$ is the projection vector of the position of the jth nucleon in the target nucleus on the ₉₂ x-y plane (the beam direction being the z-axis), Γ_{NN} is the $_{93}$ nucleon-nucleon (NN) profile function, which is the Fourier ₉₄ transform of the NN scattering amplitude, and $|\Phi_0\rangle$ is the 95 wave function of the target nucleus, which has a mass num- $_{96}$ ber A_{T} . When an independent particle model wave function 97 is used, which is usually assumed in Glauber model calcula-98 tions, the density of the target nucleus can be written as[14]:

$$|\Phi_0^{\mathrm{T}}(\boldsymbol{r}_1, \boldsymbol{r}_2, \cdots, \boldsymbol{r}_{A_{\mathrm{T}}})|^2 = \prod_{j=1}^{A_{\mathrm{T}}} n_j(\boldsymbol{r}_j),$$
 (2)

where $n_i(\mathbf{r}_i)$ stands for the normalized density distribution of the jth nucleon in the target nucleus. The nucleon density distribution is then

$$\rho_{\mathrm{T}}(\mathbf{r}) = \sum_{j=1}^{A_{\mathrm{T}}} n_j(\mathbf{r}). \tag{3}$$

With an uncorrelated wave function satisfying Eq. 2, the nucleon-target phase shift function has the form [14]:

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$$e^{i\chi_{NT}(\boldsymbol{b})} = \prod_{j=1}^{A_{\mathrm{T}}} \left[1 - \int d\boldsymbol{r} n_{j}(\boldsymbol{r}) \Gamma_{NN}(\boldsymbol{b} - \boldsymbol{t}) \right], \quad (4)$$

64 section II; results of our calculations are given in section III, 107 where t is the projection of r on the x-y plane. When the

$$1 - \int d\mathbf{r} n_j(\mathbf{r}) \Gamma_{NN}(\mathbf{b} - \mathbf{t}) \approx e^{-\int d\mathbf{r} n_j(\mathbf{r}) \Gamma_{NN}(\mathbf{b} - \mathbf{t})}. \quad (5)$$

One then gets the nucleon-target phase shift of the OLA [14]:

$$e^{i\chi_{NT}^{OLA}(\boldsymbol{b})} = \prod_{j=1}^{A_{T}} \exp\left[-\int d\boldsymbol{r} n_{j}(\boldsymbol{r}) \Gamma_{NN}(\boldsymbol{b} - \boldsymbol{t})\right]$$

$$= \exp\left[-\sum_{j=1}^{A_{T}} \int d\boldsymbol{r} n_{j}(\boldsymbol{r}) \Gamma_{NN}(\boldsymbol{b} - \boldsymbol{t})\right]$$

$$= \exp\left[-\int d\boldsymbol{r} \rho_{T}(\boldsymbol{r}) \Gamma_{NN}(\boldsymbol{b} - \boldsymbol{t})\right]. \quad (6)$$

This results in the nucleon-nucleus phase-shift function using 118 the OLA being:

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$$\chi_{NT}^{\mathrm{OLA}}(\boldsymbol{b}) = i \int d\boldsymbol{r} \rho_T(\boldsymbol{r}) \Gamma_{NN}(\boldsymbol{b} - \boldsymbol{t}).$$
 (7)

120 Note that in Eqs. (1) and (4), multiple scattering terms ap-121 pear through cumulant expansions of the phase-shift func-122 tions. However, after applying the approximation of Eq. (5) in Eq. (4), the resulting nucleon-nucleus phase-shift with the 124 OLA in Eq. (7) contains no multiple scattering terms any-125 more [18].

Similar to the nucleon-nucleus case in Eq. (1), the nucleusnucleus phase shift function, $\chi_{PT}(\boldsymbol{b})$, for a composite projec-128 tile and a target nucleus is [14]:

$$e^{i\chi_{PT}(\boldsymbol{b})} = \langle \Phi_0^{P} \Phi_0^{T} | \prod_{i=1}^{A_{P}} \prod_{j=1}^{A_{T}} [1 - \Gamma_{NN}(\boldsymbol{b} + \boldsymbol{s}_i - \boldsymbol{t}_j)] | \Phi_0^{P} \Phi_0^{T} \rangle,$$
(8)

where Φ_0^P is the many-body wave functions of the projectile 131 (with a mass number $A_{\rm P}$) in its ground state. The integrals are over the coordinates of all the nucleons i and j in the projectile and target nuclei, whose coordinates are r_i and r_j , respec-134 tively. s_i , and t_j are their projections on the x-y plane. The 135 nucleus-nucleus phase shift in this equation contains contributions from single collisions and all order multiple scattering among the constituent nucleons in the projectile and the target 138 nuclei. Equation (8) is cumbersome to evaluate directly even 139 if it is possible. So the optical limit approximation is usually (3) 140 used and the phase shift function with this approximation is 141 [14]:

$$\chi_{\text{PT}}^{\text{OLA}}(\boldsymbol{b}) = i \int d\boldsymbol{r}_{\text{P}} \rho_{\text{P}}(\boldsymbol{r}_{\text{P}}) \int d\boldsymbol{r}_{\text{T}} \rho_{\text{T}}(\boldsymbol{r}_{\text{T}}) \Gamma_{NN}(\boldsymbol{b} + \boldsymbol{s} - \boldsymbol{t}),$$
(9)

where $ho_{
m P}$ and $ho_{
m T}$ are the nucleon density distributions of the (4) 144 projectile and the target nuclei, respectively, $r_{\rm P}$ and $r_{\rm T}$ are 145 the positions of their constituent nucleons, whose projections 147 nucleus case in Eq. (7), only single NN collisions contribute 184 (12), the NTG phases shift will reduce to that of the OLA in 148 to this phase shift. Contributions from multiple scatterings 185 Eq. (9). By taking into account the higher order terms in Eq. 149 are missing, which could be, to some extent, recovered by 186 (15), phase shifts with the NTG model recover some multiple 150 the nucleon-target version of the Glauber model (the NTG 187 scattering effects that are missing with the OLA. One should model) proposed by Abu-Ibrahim and Suzuki [14–17].

153 $\Gamma_{NN}(m{b}+m{s}_i-m{t}_i)]|\Phi_0^{
m T}
angle$ for each nucleon i in the projectile in 190

$$\langle \Phi_0^{\mathrm{T}} | \prod_{j=1}^{A_{\mathrm{T}}} [1 - \Gamma_{NN}(\boldsymbol{b} + \boldsymbol{s}_i - \boldsymbol{t}_j)] | \Phi_0^{\mathrm{T}} \rangle$$

$$\equiv 1 - \Gamma_{NT}(\boldsymbol{b} + \boldsymbol{s}_i), \tag{10}$$

where $\Gamma_{NT}\left(m{b}+m{s}_{i}
ight)$ is the profile function of its collision 158 with the target nucleus. The nucleus-nucleus phase shift then $_{159}$ takes the form [14]:

$$e^{i\chi_{PT}^{NTG}(\boldsymbol{b})} = \langle \Phi_0^{P} | \prod_{i=1}^{A_P} [1 - \Gamma_{NT} (\boldsymbol{b} + \boldsymbol{s}_i)] | \Phi_0^{P} \rangle.$$
 (11)

161 This is the so-called NTG model. Following the same procedure of obtaining the Eq. (7), the phase shift of the projectiletarget system with the NTG model is:

$$\chi_{PT}^{\rm NTG}(\boldsymbol{b}) = i \int d\boldsymbol{r} \rho_{\rm P}(\boldsymbol{r}) \Gamma_{NT}(\boldsymbol{b} + \boldsymbol{s}), \tag{12}$$

and the nucleon-target profile function, Γ_{NT} is:

166
$$\Gamma_{NT}(\boldsymbol{b}+\boldsymbol{s}_i)$$
167
$$=1-\langle\Phi_0^{\mathrm{T}}|\prod_{j=1}^{A_{\mathrm{T}}}\left[1-\Gamma_{NN}(\boldsymbol{b}+\boldsymbol{s}_i-\boldsymbol{t}_j)\right]|\Phi_0^{\mathrm{T}}\rangle$$
168
$$=1-\exp\left[-\int d\boldsymbol{r}_T\rho_T(\boldsymbol{r}_T)\Gamma_{NN}(\boldsymbol{b}+\boldsymbol{s}-\boldsymbol{t})\right]. (13) \ _{209}^{208}$$

Substituting this Γ_{NT} in Eq. (12), we get the nucleus-nucleus 170 phase shift function of the NTG model:

171
$$\chi_{PT}^{
m NTG}(m{b}) = i \int dm{r}_{
m P}
ho_{
m P}(m{r}_{
m P})$$
172 $\times \left\{ 1 - \exp\left[-\int dm{r}_{
m T}
ho_{
m T}(m{r}_{
m T}) \Gamma_{NN}(m{b} + m{s} - m{t}) \right] \right\} (14)$

That the nucleus-nucleus phase shift of the NTG model 174 contains multiple scattering effects other than the OLA can be seen by power expansion of the nucleon-target profile func-176 tion of Eq. (13):

177
$$\Gamma_{NT}(\boldsymbol{b}+\boldsymbol{s}_i)$$
178
$$=\int d\boldsymbol{r}_T \rho_T(\boldsymbol{r}_T) \Gamma_{NN}(\boldsymbol{b}+\boldsymbol{s}-\boldsymbol{t}) -$$
179
$$\frac{1}{2!} \left[\int d\boldsymbol{r}_T \rho_T(\boldsymbol{r}_T) \Gamma_{NN}\left(\boldsymbol{b}+\boldsymbol{s}-\boldsymbol{t}\right)\right]^2 + \cdots . \quad (15)$$

181 jectile nucleon from nucleons in the target nucleus. The sec- 228 this work, our main purpose is to study how much the single-182 ond and other terms represent contributions from multiple NN 229 nucleon removal cross sections (σ_{-1N}) will change when the

146 on the x-y plane are s and t respectively. As in the nucleon- 183 scattering [14]. Clearly, if only the first term is used in Eq. 188 note, however, that the contributions from multiple scattering The idea of the NTG model is to replace $\langle \Phi_0^{\rm T} | \prod_{j \in {
m T}} [1-{
m _{189}}$ processes included in this way is not identical to those in full Glauber model in Eqs. (1) and (8) [19]. Nevertheless, as we will show in the next section, the NTG model could improve 192 the description of the elastic scattering angular distributions, 193 especially at low incident energies, and total reaction cross sections for the ¹²C+¹²C test case within a rather wide range 195 of incident energies. Practically, a symmetrized version of the 196 NTG phase shift is often calculated [15, 17]:

$$\chi_{PT}^{NTG}(\boldsymbol{b}) = \frac{i}{2} \int d\boldsymbol{r}_{P} \rho_{P}(\boldsymbol{r}_{P}) \Big\{ 1 - \exp \Big[- \int d\boldsymbol{r}_{T} \rho_{T}(\boldsymbol{r}_{T}) \Gamma_{NN}(\boldsymbol{b} + \boldsymbol{s} - \boldsymbol{t}) \Big] \Big\}$$

$$+ \frac{i}{2} \int d\boldsymbol{r}_{T} \rho_{T}(\boldsymbol{r}_{T}) \Big\{ 1 - \exp \Big[- \int d\boldsymbol{r}_{P} \rho_{P}(\boldsymbol{r}_{P}) \Gamma_{NN}(\boldsymbol{b} + \boldsymbol{t} - \boldsymbol{s}) \Big] \Big\}.$$
(16)

 $_{\rm 202}$ However, the phase-shifts calculated with Eqs. (14) and (16) $_{\rm 203}$ are often very close to each other [15, 16].

The profile function Γ_{NN} in the both the OLA and the NTG model calculations is parameterized in a Gaussian form:

$$\Gamma_{pN}(\mathbf{b}) = \frac{1 - i\alpha_{pN}}{4\pi\beta_{pN}} \sigma_{pN}^{\text{tot}} \exp\left(-\frac{\mathbf{b}^2}{2\beta_{pN}}\right),$$
 (17)

where the Γ_{NN} parameters $\sigma_{pN}^{\rm tot}$, α_{pN} , and β_{pN} are the proton-nucleon total cross section, the ratio of the real to imaginary part of the p-N scattering amplitudes, and the corresponding slope parameter [20], respectively. Due to the lack of experimental data on neutron-neutron scattering, Γ_{pp} 212 is commonly used instead of Γ_{NN} . In this work, σ_{nN}^{tot} are taken from Ref. [21], which is parameterized by fitting the experimental data from Ref. [22], the α_{pN} parameters are taken 215 from those tabulated from Ref. [20] for a range of incident energies from 100 to 2200 MeV/u. If the beam energy is lower 217 than 100 MeV/u, we take the value corresponding to lowest 218 energy from the table. The finite range slope parameters β_{pN} 219 are taken to be 0.125 fm², in accordance with systematic stud-220 ies of single-nucleon removal reaction[10, 12, 23].

COMPARISONS BETWEEN THE NTG MODEL AND **OLA IN GLAUBER MODEL CALCULATIONS**

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In Ref. [24], T. Nagashisa and W. Horiuchi demonstrated $\frac{1}{2!} \left[\int d\mathbf{r}_T \rho_T(\mathbf{r}_T) \Gamma_{NN} \left(\mathbf{b} + \mathbf{s} - \mathbf{t} \right) \right]^2 + \cdots . \quad \text{(15)} \quad \text{224 the effectiveness of the NTG by comparing the description} \\ \text{225 of the total reaction cross sections using the full Glauber}$ 226 model calculation, the NTG model, and the OLA for cases 180 The first term is contributed by single scattering of the pro- 227 of ^{12,20,22}C on a ¹²C target at various incident energies. In

230 NTG model instead of the OLA is used. Before calculating 260 total reaction cross sections of the ¹²C+¹²C system is shown σ_{-1N} , we need to firstly compare our calculations for the σ_{-1N} in Fig. 2. Again, we see that results of the NTG model have 232 elastic scattering angular distributions and total reaction cross 262 better agreement with the experiment data than those of the 233 sections with experimental data and with the predictions of 263 OLA, especially for the incident energies at several tens of the OLA. The calculations are made for the ¹²C+¹²C system. ²⁶⁴ MeV/nucleon and above, where most of the one-nucleon re-By doing so, we also verify the effectiveness of the Γ_{NN} pa- 265 moval cross section data were measured [9]. In both elasrameters used in our calculations, which are further used in 286 tic scattering and total reaction cross section calculations, the code MOMDIS [25].

Elastic scattering angular distributions and total reaction cross sections

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The angular distributions of ¹²C elastic scattering from a ¹²C target at 30, 85, 120, and 200 MeV/nucleon are calculated with both the OLA and the NTG model. The results are shown in Fig. 1 together with the experimental data. Clearly, the NTG improved the description of the ¹²C+¹²C elastic scattering considerably with respect to the OLA, especially when the incident energy is below around 100 MeV/nucleon. which are included in the NTG model but not in the OLA, should be more important at low incident energies than at higher incident energies. Note that other corrections due to, 253 for instance, the antisymmetrization of the projectile and target wavefunctions [26], the Fermi motion of the nucleons in the colliding nuclei [27], distortion of the trajectories [28], can also affect the low-energy cross sections. More complete 257 calculations taking these aspect together might be an interest-258 ing subject for future.

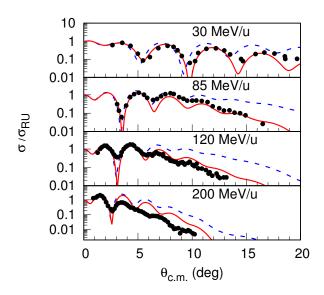


Fig. 1. Elastic scattering angular distributions of ¹²C on a carbon target at incident energies of 30, 85, 120, and 200 MeV/nucleon. The red solid and blue dashed curves are results of Glauber model dots are experimental data from Refs. [29, 30].

the calculations of σ_{-1N} . The single-nucleon removal reac- 267 proton and neutron density distributions of the 12 C nucleus tions are calculated using a modified version of the computer 288 are taken to be a Gaussian form with a root-mean-square ra-269 dius of 2.32 fm [9], which is very close to the 2.33 ± 0.01 fm 270 from elastic electron scattering data [31].

Note that the Γ_{NN} parameters are the same in both NTG 272 and OLA calculations. The only difference between these 273 two methods is that the former introduced multiple scattering 274 effects in the calculation of eikonal phase functions. The im-275 provement provided by the NTG model in the description of 276 elastic scattering angular distributions and the total reaction 277 cross sections suggests that nuclear medium effects, such as 278 the multiple scattering effect studied here, should be taken 279 into account in Glauber model description of the nuclear re-280 actions induced by heavy-ions. In the following section, we 281 study how the NTG model could affect the theoretical pre-This can be expected because the multiple scattering effect, 282 dictions of the single-neutron removal cross sections and the 283 single particle strengths obtained from the experimental data.

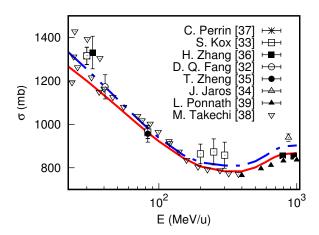


Fig. 2. Reaction cross sections of ¹²C on a carbon target. The red solid and blue dash-dotted curves are results of Glauber model calculations with the NTG model and the OLA, respectively. The symbols represent experimental data from Ref. [32–39].

Single-nucleon removal cross sections at different incident energies

In an inclusive single-nucleon removal reaction, A(a, b)X, where only the core nucleus b ($A_b = A_a - 1$) is detected, two calculations with the NTG model and the OLA, respectively. The 288 processes may happen: the diffraction dissociation and strip-289 ping, which correspond to the valence neutron escaped or be-290 ing captured by the target nucleus, respectively. Within the Comparison between the NTG and OLA predictions to the 291 Glauber model framework, their cross sections, $\sigma_{sp}^{\rm dd}$ and $\sigma_{sp}^{\rm str}$

292 respectively, are calculated by: [40]:

$$\sigma_{sp}^{\rm dd} = \frac{1}{2j+1} \sum_{m} \int d\mathbf{b} \left[\left\langle \psi_{nljm} \left| \left| 1 - S_{v} S_{c} \right|^{2} \right| \psi_{nljm} \right\rangle \right.$$

$$-\sum_{m'} |\langle \psi_{nljm'} | (1 - S_v S_c) | \psi_{nljm} \rangle|^2 \bigg], \qquad (18)$$

295 and

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$$\sigma_{sp}^{\text{str}} = \frac{1}{2j+1} \sum_{m} \int d\mathbf{b} |S_{c}|^{2} \times \left\langle \psi_{nljm} \left| \left(1 - \left| S_{v} \right|^{2} \right) \right| \psi_{nljm} \right\rangle. \tag{19}$$

Here $S_c=e^{i\chi_{cT}}$ and $S_v=e^{i\chi_{vT}}$ are the core-target and the valence nucleon-target S-matrices, respectively. The valence nucleon-target phase shift function χ_{vT} is calculated with Eq. (7), and the core-target phase shift function χ_{cT} is calculated according to Eq. (9) for the OLA and Eq. (16) for the NTG model; \boldsymbol{b} is the impact factor vector of the projectile in the plane perpendicular to the beam direction, ψ_{nljm} is the single-particle wave function (SPWF) with n, l, and j being the principal, the angular momentum, and the total angular momentum numbers respectively, and m is the projection of j. Equations (7, 9, 14 and 16) are about nuclear phaseshift only. For charged particles, one also has to include the Coulomb phase-shift [25]:

$$\chi_{\rm C} = 2\eta \ln(kb), \tag{20}$$

where $\eta=Z_1Z_2e^2\mu/\hbar^2k$ is the Sommerfeld parameter with Z_1 and Z_2 being the charge numbers of the two colliding particles, whose reduced mass is μ , and Z_2 being the wave numbers in the center of mass system. The single-particle wave functions are associated with the specific states of the core with spin Z_2 with spin Z_3 and the composite nuclei with spin Z_3 by spectroscopic factors, $(C^2S)_{Z_aI_b,nlj}$. So, the single-particle cross section of removal of a nucleon from the ground state of a projectile leaving the core nucleus in a specific state with the SPWF having quantum numbers Z_3 is:

$$\sigma_{sp}(I_a I_b, n l j) = \left(\frac{\mathbf{A}}{\mathbf{A} - 1}\right)^N \left(C^2 S\right)_{I_a I_b, n l j} \times \left(\sigma_{sp}^{dd} + \sigma_{sp}^{str}\right),$$
(21)

where the $[A/(A-1)]^N$ factor is for the center-of-mass corsections to the spectroscopic factor C^2S [41], and N=2n+l is the number of oscillator quanta associated with the major shell of the removed particle (the minimum value of n is taken to be zero).

Experimentally, single-nucleon removal cross sections are usually measured inclusively, namely, only the core nucleus b is measured without discriminating its energy states. Correspondingly, theoretical calculations for these measurements should also include the contributions from all the bound excited states of the core nucleus b [10], which corresponds to summation of all the single-particle cross sections associated with all possible single particle wave functions:

$$\sigma_{-1N}^{\text{th}} = \sum_{nlj,I_b} \sigma_{sp}(I_a I_b, nlj). \tag{22}$$

TABLE 1. Single neutron removal cross sections of $^{19}\mathrm{C}$ on a beryllium target at incident energies of 64, 100, 200, and 400 MeV/nucleon calculated with the NTG model, $\sigma_{-1n}^{\mathrm{NTG}}$, and the OLA, $\sigma_{-1n}^{\mathrm{OLA}}$. The state of the core nucleus and their corresponding single-nucleon spectroscopic factors are taken from Ref. [12].

$E_{ m inc}$	E_x	J^{π}	nlj	C^2S	$\sigma_{-1n}^{\mathrm{OLA}}$	$\sigma_{-1n}^{\rm NTG}$	$\sigma_{-1n}^{ m NTG}/\sigma_{-1n}^{ m OLA}$
64	0.000	0+	$1s_{1/2}$	0.580	104.31	109.3	1.050
	2.144	2^{+}	$0d_{5/2}$	0.470	18.93	21.16	1.118
	3.639	2^+	$0d_{5/2}$	0.104	3.53	3.98	1.127
	3.988	0_{+}	$1s_{1/2}$	0.319	17.82	19.72	1.107
	4.915	3^+	$0d_{5/2}$	1.523	46.18	52.21	1.131
	4.975	2^+	$0d_{5/2}$	0.922	27.83	31.46	1.130
	Inclusive				218.42	237.83	1.089
100	0.000	0_{+}	$1s_{1/2}$	0.580	87.58	90.14	1.029
	2.144	2^+	$0d_{5/2}$	0.470	17.95	19.13	1.066
	3.639	2^+	$0d_{5/2}$	0.104	3.41	3.64	1.067
	3.988	0_{+}	$1s_{1/2}$	0.319	16.43	17.44	1.061
	4.915	3^+	$0d_{5/2}$	1.523	45.05	48.24	1.071
	4.975	2^+	$0d_{5/2}$	0.922	27.15	29.08	1.071
	Inclusive				197.57	207.67	1.051
200	0.000	0+	$1s_{1/2}$	0.580	61.66	63.55	1.031
	2.144	2^{+}	$0d_{5/2}$	0.470	15.46	16.52	1.069
	3.639	2^+	$0d_{5/2}$	0.104	3.01	3.23	1.073
	3.988	0_{+}	$1s_{1/2}$	0.319	13.47	14.30	1.062
	4.915	3+	$0d_{5/2}$	1.523	40.59	43.61	1.071
	4.975	2^+	$0d_{5/2}$	0.922	24.48	26.31	1.075
	Inclusive				158.67	167.52	1.056
400	0.000	0+	$1s_{1/2}$	0.580	54.76	57.04	1.042
	2.144	2^{+}	$0d_{5/2}$	0.470	14.61	16.00	1.095
	3.639	2^{+}	$0d_{5/2}$	0.104	2.87	3.16	1.101
	3.988	0_{+}	$1s_{1/2}$	0.319	12.54	13.57	1.082
	4.915	3^+	$0d_{5/2}$	1.523	38.80	42.91	1.106
	4.975	2^+	$0d_{5/2}$	0.922	23.41	25.89	1.106
	Inclusive				146.99	158.57	1.079

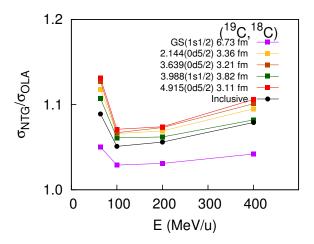


Fig. 3. Ratios of the NTG and OLA predicted single particle cross sections associated with different core states of the $^9\mathrm{Be}(^{19}\mathrm{C},^{18}\mathrm{C})\mathrm{X}$ reaction at incident energies 64, 100, 200, and 400 MeV/nucleon. The black dots represent the results calculated with Eq. (22). The excitation energies of the core nucleus $^{18}\mathrm{C}$ and the properties of their corresponding single-particle wave functions – their nlj values and root-mean-square radii – are also shown. The lines are to guide eyes.

In order to see how much difference the NTG model pre-338 dicts the single-nucleon removal cross sections with respect 339 to the OLA, we study the (19C, 18C) reaction on a 9Be target at 64, 100, 200, and 400 MeV/nucleon incident energies. The excited states of the ¹⁸C nucleus, the associated single particle wave functions, and their corresponding shell model predicted spectroscopic factors are taken to be the same as those in Ref. [12]. The single particle wave functions are calculated with single particle potentials of Woods-Saxon forms with the depths adjusted to provide the experimental separation energies of the valence nucleon, and the radius and diffuseness parameters are taken to be $r_0 = 1.25$ fm and a = 0.7349 fm, respectively, the same as those used in Ref. [12]. The results are shown in Table. 1. Single-nucleon removal cross sections with the NTG model and the OLA are denoted as $\sigma_{-1n}^{\rm NTG}$ and $\sigma_{-1n}^{\rm OLA}$, respectively. Note that the $\sigma_{-1n}^{\rm OLA}$ values at 64 MeV/nucleon agree very well with those reported in Ref. [12]. The ratios between $\sigma_{-1n}^{\rm NTG}$ and $\sigma_{-1n}^{\rm OLA}$, are also depicted in 355

It is interesting to observe that:

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- 1. the one-nucleon removal cross sections calculated with the NTG model is larger than those with the OLA within the whole energy range from 50 to 400 MeV/nucleon,
- 2. Such differences are larger at incident energies smaller than around 100 MeV/nucleon, almost constant around 100-200 MeV/nucleon, and increase slightly when the incident energy is larger than around 200 MeV/nucleon,
- 3. The differences are also bigger when the root-meansquare radius of the single particle wave function is smaller, which means that the NTG model is especially important for one-neutron removal cross sections of a given reaction when the single nucleon is tightly bound.

The difference between the NTG model and the OLA is in 399 and the OLA, σ_{-1N}^{NTG} and σ_{-1N}^{OLA} , respectively, are also listed the core-target S-matrix, S_c , only. However, as we see from 400 together with the experimental single-nucleon removal cross 374 Eqs. (18) and (19), we are not able to separate S_c from S_v 401 sections, σ_{-1N}^{exp} , and the reduction factors, \mathfrak{R}^{NTG} and \mathfrak{R}^{OLA} , and the reduction factors, \mathfrak{R}^{NTG} and \mathfrak{R}^{OLA} , and the reduction factors \mathfrak{R}^{NTG} and \mathfrak{R}^{OLA} . 375 and the single particle wave functions in the calculation of $_{402}$ respectively. The single-particle spectroscopic factors (C^2S) NTG model instead of the OLA is used.

C. Reduction factors of single particle strengths

duction factors of the SFs, R_s , which are ratios between the 419 culations [42] and the diffuseness parameters being fixed as

experimental and theoretical SFs, are defined to quantify such differences. For the case of inclusive single-nucleon knockout reactions, the reduction factors are defined as the ratios between the experimental and theoretical cross sections [8, 9]:

$$R_s = \sigma_{-1N}^{\text{exp}}/\sigma_{-1N}^{\text{th}}$$
.

383 For nuclei that have more than one sets of experimental data available, a weighted mean of the R_s values for each mea-385 surement is used [43]:

$$\mathfrak{R} = \frac{\sum_{i} R_{si} w_i}{\sum_{i} w_i},\tag{23}$$

where the weights are defined by the errors of the individual R_s values $(\Delta R_s)_i$:

$$w_i = \left[\frac{1}{\Delta R_{si}}\right]^2,$$

and the errors of the averaged \overline{R}_s is:

$$\Delta \mathfrak{R} = \frac{1}{\sqrt{\sum_i w_i}}.$$

The effective neutron-proton asymmetry ΔS_{eff} is given 388 by[[12]]

$$\Delta S_{\text{eff}} = S_n + \bar{E}_f - S_p$$
, for neutron removal,
 $\Delta S_{\text{eff}} = S_p + \bar{E}_f - S_n$, for proton removal,

where $ar{E}_f$ is obtain by weighting the excitation energy E^* of 392 each final state by the single nucleon removal cross section to that state.

Using the method described in the previous subsection, we 395 analyzed a series of single-nucleon removal reaction data. 396 Details of these reactions, such as the target nuclei used, the 397 incident energies are given in Table. 2. The theoretical pre-371 The same are found for other nuclei studied in this work. 398 dicted single-nucleon removal cross sections using the NTG single-nucleon removal cross sections. Thus, we can not ex- 403 used in these calculations are taken from references correhibit the details how the NTG model along affects the σ_{-1n} sponding to the experimental data and Refs. [43]. These revalues with respect to the OLA. In the following subsection, 405 duction factors are depicted in Fig. 4 as functions of neutronwe study how the spectroscopic factors extracted from the ex- $_{406}$ proton asymmetry. Since many σ_{-1N} were measured inperimental data and their reduction factors change when the 407 clusively, namely, they include all bound states of the core 408 nuclei, which correspond to different separation energies of 409 the removed nucleon, an effective neutron-proton asymme-410 try is used here: $\Delta S_{\mathrm{eff}} = S_n + \bar{E}_f - S_p$ for neutron re-411 moval and $\Delta S_{\mathrm{eff}} = S_p + \bar{E}_f - S_n$ for proton removal, where 412 \bar{E}_f is the weighted mean excitation energy of the core nu-The spectroscopic factors in Eq. (22) are often taken from 413 cleus, $E_f = (\sum_i E_{\text{ex,i}} \sigma_{sp,i}) / \sum_i \sigma_{sp,i}$, with $E_{\text{ex,i}}$ and $\sigma_{sp,i}$ configuration interaction shell model (CISM) calculations in 414 being the excitation energy of the core nucleus in its i-th calculating the one-nucleon removal cross sections. Due to 415 state and the corresponding single particle cross section with limited model spaces and insufficient treatment of nucleon- 416 Eq. (21) [8]. In all these calculations, the single particle nucleon correlations, It is well-known that the CISM pre- 417 wave functions are calculated with Woods-Saxon potentials dicted SFs are usually larger than the experimental ones. Re- 418 whose radius parameters, r₀, are determined with the HF cal $_{420}~a=0.65~\mathrm{fm}$ except for the $^{15,17,18}\mathrm{C}$ projectiles, for which, $_{454}$ single proton removal reactions. From the $\mathfrak{R}^{\mathrm{NTG}}$ and $\mathfrak{R}^{\mathrm{OLA}}$ the $r_0=1.15$ fm and a=0.50 fm is used following Ref. the values shown in Table. 2, one sees that the average difference [442]. And for proton removal of 16 C, $r_0=1.40$ fm and the second shown in Table. 2, one sees that the average difference [443] and 16 C, $^{$ a = 0.70 fm is used following Ref. [45]. The proton and a = 0.70 fm is used following Ref. [45]. The proton and a = 0.70 fm is used following Ref. [45]. ⁴²⁴ neutron density distributions of the nucleus ⁹Be are taken to ⁴⁵⁸ is not clear why the effect of the NTG model has such sys-425 be a Gaussian form with a root-mean-square radius of 2.36 459 tematic differences to these two types of reactions. As we 426 fm [9].

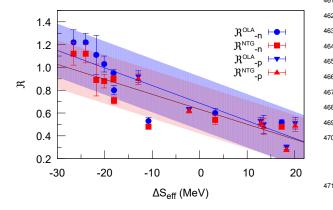


Fig. 4. Averaged reduction factors $\mathfrak R$ listed in Table. 2 as functions 472 bands represent the widths of their distributions.

428 the NTG model are generally larger than those with the OLA. 480 energy single nucleon removal cross sections as those com-490 the OLA. On average, the changes in the R values induced 482 neutron-proton asymmetry, whereas those of other types of $_{431}$ by the NTG model with respect to the OLA are about 7.8%. $_{483}$ reactions, such as (p,pN) and single nucleon transfer reactions However, as one can see from Fig. 4, that the \Re values with 484 do not [2, 3, 6, 59–61]. Since the single-nucleon removal re-433 the NTG model and the OLA, \Re^{NTG} and \Re^{OLA} , respectively, 485 actions were analyzed with the Glauber model, validity of the 434 still depend linearly on the effective neutron-proton asymme- 486 Glauber model on such reactions is being questioned. With $_{435}$ try $\Delta S_{\rm eff}$, although the slope with the NTG model is 18% $_{487}$ this respect, corrections to the Glauber model and examina-436 smaller than that with the OLA. The parameters of this linear 488 tion of their effects on the single-nucleon removal cross sec-437 dependence are:

$$\mathfrak{R}^{\text{OLA}} = 0.687 - 0.0154\Delta S_{\text{eff}},$$

$$\mathfrak{R}^{\text{NTG}} = 0.633 - 0.0131\Delta S_{\text{eff}}.$$
(24)

499 So the systematics of the $\mathfrak R$ values with respect to $\Delta S_{
m eff}$ ob-440 served in Refs. [8, 9] persist even when the multiple scat- 495 the usual optical limit approximation, which does not contain tering effects inherited in the NTG model are included in the 496 multiple scattering effects. For this purpose, we firstly exam-Glauber model calculations.

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444 ences between \mathfrak{R}^{NTG} and \mathfrak{R}^{OLA} in the most negative $\Delta S_{\rm eff}$ 499 of the $^{12}\text{C}+^{12}\text{C}$ system, and compare their results with the region are larger than at the most positive $\Delta S_{\rm eff}$ region. To 500 experimental data and those calculated with the OLA. The 446 be more specific, the averaged differences between $\mathfrak{R}^{\rm NTG}$ 501 NTG model is found to improve the description of the elastic 447 and $\mathfrak{R}^{\text{OLA}}$ is 9.9% for ΔS_{eff} < -10 MeV and 5.3% for 502 scattering angular distributions, especially at lower incident $_{448}$ $\Delta S_{
m eff} > 10$ MeV. This seems to suggest that the multiple $_{503}$ energies. Both the elastic scattering and total reaction cross 449 scattering effect introduced with the NTG model is more im- 504 sections calculated in this work agree well with those reported 450 portant for removal of weakly bound nucleons than for deeply 505 in previous publications, e.g., Refs. [15, 17, 24]. 451 bound ones. This is misleading. It happens that most of the 506 We then compare the predictions of inclusive single- $_{ ext{452}}$ cases in the $\Delta S_{ ext{eff}} < -10$ MeV region are single neutron re- $_{ ext{507}}$ nucleon removal cross sections by using the NTG model and 453 moval reactions, and those in the $\Delta S_{\rm eff} > 10$ MeV region are 508 OLA. The case studied is the ${}^9{\rm Be}({}^{19}{\rm C},{}^{18}{\rm C}){\rm X}$ reaction within

460 discussed at the end of the last section, the only difference between the NTG model and the OLA is in the core-target S-462 matrices, S_c . However, as one sees from Eqs. (18) and (19), 463 S_c can not be singled out from S_v and the single-particle wave 464 functions when calculating the single-nucleon removal cross sections. This means that the multiple scattering effects in-466 duced in the NTG model to σ_{-1N} through S_c are moderated 467 by the single particle wave functions, which are different for different cases. So we are not able to explicitly show how the 469 NTG model alone affects the σ_{-1N} values and why it behaves 470 differently for proton and neutron removal reactions.

IV. SUMMARY

The reduction of the single-particle strengths, represented of the effective neutron-proton asymmetry $\Delta S_{\rm eff}$. The red squares 473 by the reduction factors of single-nucleon spectroscopic facand blue dots are results of the neutron removal of the NTG model 474 tors extracted from experimental data with respect to conand the OLA, respectively. The red triangles and blue inverted tri- 475 figuration interaction shell model predictions, is supposed to angles are the same but for proton removal. The light red and blue 476 be related to the nucleon-nucleon correlations in atomic nu-477 clei. Quite a lot of theoretical and experimental efforts have 478 been devoted to this area. One of the open questions is why As one can see from Table. 2, σ_{-1N} values predicted with 479 the reduction factors obtained from intermediate- and high-Thus, the R values with the NTG are smaller than those with 481 piled in Refs. [8, 9] show strong linear dependence on the 489 tions become important.

In this work, we examine how the nucleon-target version 491 of the Glauber model (the NTG model), which introduces 492 multiple scattering of the constituent nucleons in the projec-493 tile and the target nuclei, could change the theoretical pre-497 ined the NTG model in its reproduction of the elastic scatter-Looking more closely at Fig. (4), one sees that the differ- 498 ing angular distributions and the total reaction cross sections

TABLE 2. Experimental $(\sigma_{-1N}^{\rm exp})$ and theoretical inclusive single-nucleon removal cross sections calculated with the OLA $(\sigma_{-1N}^{\rm OLA})$ and the NTG model $(\sigma_{-1N}^{\rm NTG})$, and the corresponding reductions factors $\mathfrak{R}^{\rm OLA}$ and $\mathfrak{R}^{\rm NTG}$.

Reaction	$\Delta S_{ m eff}$	Target	$E_{ m inc}$	$\sigma^{ m exp}_{-1N}$	$\sigma_{-1N}^{ m OLA}$	$\sigma_{-1N}^{ m NTG}$	$\mathfrak{R}^{\mathrm{OLA}}$	$\mathfrak{R}^{ ext{NTG}}$
(²⁰ C, ¹⁹ C)	-26.574	С	240	58(5) [46]	47.55	51.88	1.22(11)	1.12(10)
$(^{19}C,^{18}C)$	-24.142	Be	57	264(80) [47]	179.06	201.62	1.47(45)	1.31(40)
, ,	-24.104	Be	64	226(65) [48]	176.69	195.48	1.28(37)	1.16(33)
	-23.754	C	243	163(12) [46]	134.75	146.63	1.21(9)	1.11(8)
Average	-24.022			, , , , ,			1.22(8)	1.12(8)
$(^{18}C,^{17}C)$	-21.793	C	43	115(18) [44]	103.20	128.70	1.11(17)	0.89(14)
$(^{17}C,^{16}C)$	-20.130	C	49	84(8) [44]	92.80	109.70	0.91(9)	0.77(7)
	-20.121	Be	62	115(14) [47]	87.80	100.77	1.31(16)	1.14(14)
	-20.121	Be	79	116(18) [49]	90.37	100.48	1.28(20)	1.15(18)
Average	-20.124			, , , , ,			1.03(7)	0.88(6)
$(^{15}C,^{14}C)$	-18.275	C	54	137(16) [44]	180.56	196.44	0.76(9)	0.70(8)
, ,	-18.242	C	62	159(15) [44]	176.11	189.78	0.90(8)	0.84(8)
	-18.169	C	83	146(23) [32]	166.44	176.08	0.88(14)	0.83(13)
	-17.879	Be	103	146(23) [48]	142.52	149.89	0.98(3)	0.94(3)
Average	-18.155						0.95(3)	0.90(0)
$(^{16}C,^{15}C)$	-18.055	C	55	65(6) [44]	90.90	103.73	0.72(7)	0.63(6)
	-18.053	C	62	77(9) [44]	89.78	101.10	0.86(10)	0.76(9)
	-18.045	Be	75	81(7) [45]	81.99	90.94	0.99(9)	0.89(8)
	-18.094	C	83	65(5) [47]	86.75	94.87	0.75(6)	0.69(5)
Average	-18.051			. , , , ,			0.80(4)	0.71(3)
$(^{14}C,^{13}C)$	-10.807	C	67	65(4) [44]	133.284	148.61	0.49(3)	0.44(3)
	-10.800	C	83	67(14) [32]	130.74	142.66	0.51(13)	0.47(12)
	-10.767	C	235	80(7) [52]	110.92	121.39	0.72(6)	0.66(6)
Average	-10.793						0.53(3)	0.48(2)
$(^{12}C,^{11}C)$	3.259	C	95	53(22) [55]	102.21	111.06	0.52(22)	0.48(20)
, ,	3.266	C	240	60.51(11.08) [56]	94.12	104.37	0.64(12)	0.58(11)
	3.265	C	250	56.0(41) [54]	93.73	104.31	0.60(4)	0.54(4)
Average	3.263			. , , , ,			0.60(4)	0.54(4)
(10C,9C)	17.277	Be	120	23.4(11) [57]	47.40	51.65	0.49(2)	0.45(2)
, , ,	17.277	C	120	27.4(13) [57]	49.72	54.36	0.55(3)	0.50(2)
Average	17.277			, , , -			0.52(2)	0.48(2)
$({}^{9}C, {}^{8}B)$	-12.925	Be	67	48.6(73) [50]	62.77	66.67	0.77(12)	0.73(11)
	-12.925	Be	100	56(3) [51]	58.77	59.72	0.95(5)	0.94(5)
Average	-12.925						0.92(5)	0.90(5)
$(^{12}C,^{11}B)$	-2.237	C	230	63.9(66) [53]	103.75	105.33	0.62(6)	0.61(6)
	-2.237	C	250	65.6(26) [54]	102.93	105.36	0.64(3)	0.62(2)
Average	-2.237						0.63(2)	0.62(2)
$(^{13}C,^{12}B)$	13.523	C	234	39.5(60) [53]	79.69	81.55	0.43(5)	0.40(4)
$(^{14}C,^{13}B)$	12.830	C	235	41.3(27) [53]	78.65	81.43	0.53(3)	0.51(3)
$(^{16}C,^{15}B)$	18.303	Be	75	18(2) [45]	60.23	62.50	0.30(3)	0.29(3)
	18.303	Be	239	16(2) [58]	56.86	58.45	0.28(4)	0.27(3)
	18.303	C	239	18(2) [53]	54.57	55.87	0.33(4)	0.32(4)
Average	18.303			. ,			0.30(2)	0.28(2)
$(^{15}C,^{14}B)$	20.134	C	237	28.4(28) [53]	55.36	57.58	0.51(5)	0.49(5)

510 found that the σ_{-1n} values predicted with the NTG model are 526 metry of the reduction factors persists. Thus, the question of 511 larger than those predicted with the OLA within the whole 527 why the reduction factors of the single particle strengths from 512 energy range. The difference is found to be larger at lower 528 single-nucleon removal reaction measurements depend differ-513 incident energies. It will also be larger when the separation 529 ently on ΔS with respect to other types of reactions remains energy of the nucleon is larger, which correspond to a smaller 500 open even when the multiple scattering effect is included in root-mean-square radius of the single-particle wave function. 531 the Glauber model analysis with the NTG model. 515 Finally, we study how much the reduction factors of the single particle strengths obtained from single-nucleon re- $_{518}$ moval reactions change when the NTG model is used instead $_{532}$ of the OLA. The cases studied are one-nucleon removal reactions induced by $^{9-20}\mathrm{C}$ isotopes on carbon and $^{9}\mathrm{Be}$ targets. $_{533}$ On average, the reduction factors obtained with the NTG 594 R&D Program of China (Grant No. 2023YFA1606702) model are found to be less than those with the OLA by 7.8%. 535 and the National Natural Science Foundation of China (Nos. We also found that the averaged differences in σ_{-1n} are larger 596 U2067205 and 12205098). We thank Profs. J.A. Tostevin and than those in σ_{-1p} , which are 10.6% and 4.2%, respectively. 537 W. Horiuchi for their helps during this work.

509 the incident energy range from 64 to 400 MeV/nucleon. It is 525 However, the linear dependence on the neutron-proton asym-

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